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## CLASSIFIER PGN: CLASSIFICATION WITH HIGH CONFIDENCE RULES

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ABSTRACT. Associative classifiers use a set of class association rules, generated from a given training set, to classify new instances. Typically, these techniques set a minimal support to make a first selection of appropriate rules and discriminate subsequently between high and low quality rules by means of a quality measure such as confidence. As a result, the final set of class association rules have a support equal or greater than a predefined threshold, but many of them have confidence levels below 100%. PGN is a novel associative classifier which turns the traditional approach around and uses a confidence level of 100% as a first selection criterion, prior to maximizing the support. This article introduces PGN and evaluates the strength and limitations of PGN empirically. The results are promising and show that PGN is competitive with other well-known classifiers.

**1. Introduction.** Within the data mining community, research on classification techniques has a long and fruitful history. Classification techniques based on association rules, called associative classifiers (AC), are relatively new.

ACM Computing Classification System (1998): H.2.8, H.3.3.

Key words: Association rules, classification, high confidence rules.

Associative classifiers generate a set of association rules from a given training set and use these rules to classify new instances. In 1998, Liu et al. [16] introduced CBA, often considered to be the first associative classifier. During the last decade, various other associative classifiers were introduced, such as CMAR [15], ARC-AC [4], ARC-BC [4], CPAR [27], CorClass [29], ACRI [22], TFPC [7], HARMONY [25], MCAR [24], 2SARC1 [5], 2SARC2 [5], CACA [23] and ARUBAS [9].

Typically, the generation of association rules from a training set is guided by the support and confidence metrics. Many associative classifiers set a minimum support level and use the confidence metric to rank the remaining association rules. This approach, with a primary focus on support and confidence as the second criterion, will reject 100% confidence rules if the support is too low.

In this article, we question this common approach which prioritizes support over confidence. We study a new associative classifier algorithm, called PGN, which turns the priorities around and focuses on confidence first by retaining only 100% confidence rules. The main goal of this research is to verify the quality of the confidence-first concept. We therefore did not focus on the computational efficiency in this paper, which is left for future research in case the confidence-first concept is supported empirically.

The next section will introduce the related research and positions our approach into the academic literature of associative classification. Next, Section 3 explains the different steps of the PGN algorithm, while Section 4 discusses the results from the empirical analysis of PGN. Finally, conclusions and ideas for future research are stated in Section 5.

2. Associative Classifiers. Associative Classifiers are classification methods which belong to the domain of Data Mining. Fayyad et al. [10] identify Data Mining as the essential step in Knowledge Discovery process where intelligent methods are applied in order to extract data patterns. According to the taxonomy given by Maimon and Rokach [17], data mining methods can be divided into verification methods and discovery methods. Verification methods deal with the evaluation of a hypothesis proposed by an external source, while discovery methods try to identify patterns in data.

Associative Classifiers belong to the family of discovery methods, and more in particular to the predictive discovery methods. Among the predictive discovery methods, one can discern classification and estimation methods. Estimation methods map the input space onto a real-valued domain and are used when the outcome or predicted variable is continuous. Classification methods, to which associative classifiers belong, map the input space onto predefined classes and they are used when the outcome or predicted variable is categorical or nominal. Other types of classification methods or classifiers are Support Vector Machines [6], Decision Trees [20, 21], k-Nearest-Neighbor classifiers [3] and Neural Networks.

Compared to other classification methods, associative classifiers hold some interesting advantages [28]. Firstly, high dimensional training sets can be handled with ease and no assumptions are made about the dependencies between attributes. Secondly, the classification is often very fast. Thirdly, the classification model is a set of rules which can be edited and interpreted by human beings. On the other hand, associative classifiers cannot handle continuous attributes and assumes that all data are nominal or categorical. Therefore, when the data set contains continuous variables, these variables need to be discretized during data preprocessing. Discretization partitions continuous variables into a number of sub-ranges and transforms each sub-range into a category.

As mentioned in the introduction, various authors have introduced their own associative classifier algorithm over the last years. Although each implementation differs, a common structure of three consecutive steps can be identified, i.e. the association rule mining step, the pruning step (optional) and the classification step. Next, we will provide a short discussion of the various implementations of these three steps in associative classifiers.

**2.1.** Association Rule Mining. All associative classifiers start by generating association rules from a given training set. Association rule mining was first introduced in [1] and tries to extract interesting correlations, frequent patterns and associations among sets of instances in a transactional or other dataset. Originally, association rule mining focused on the analysis of transactional database, where each record represents a transaction comprising a set of items. From the transactional data perspective, the notation from [12] can be used to describe association rules.

Let **D** be a set of items, then  $X = \{i_1, \ldots, i_k\} \subseteq \mathbf{D}$  denotes an itemset or a k-itemset. A transaction over **D** is a couple  $T = \{tid, I\}$  where *tid* is the transaction identifier and *I* is an itemset. A transaction  $T = \{tid, I\}$  is said to support an itemset  $X \subseteq \mathbf{D}$  if  $X \subseteq I$ .

A transactional database D over  $\mathbf{D}$  is a set of transactions over  $\mathbf{D}$ . The cover of an itemset X in D consists of the set of transaction identifiers of transactions in D that support  $X : cover(X, D) = \{tid|(tid, I) \in D, X \subseteq I\}$ . The support of an itemset X in D is the number of transactions in the cover of X in D, i.e. support(X, D) = |cover(X, D)|. Note that  $|D| = support(\{\}, D)$ . An

itemset is called frequent if its support is no less than a given absolute minimal support threshold MinSup, with  $0 \leq MinSup \leq |D|$ .

An association rule is an expression of the form  $X \Rightarrow Y$ , where X and Y are itemsets, and  $X \cap Y = \{\}$ . Such a rule expresses the association that if a transaction contains all items in X, then that transaction also contains all items in Y. X is called the body or antecedent, and Y is called the head or consequent of the rule. The support of an association rule  $X \Rightarrow Y$  in D, is the support of  $X \cup Y$  in D and can be interpreted as a measure of evidence that the rule  $X \Rightarrow Y$  is real and not a noise artifact. The confidence or accuracy of an association rule  $X \Rightarrow Y$  in D is the conditional probability of having Y contained in a transaction, given that X is contained in that transaction, i.e.  $confidence(X \Rightarrow Y, D) = P(Y|X) = \frac{support(X \cup Y, D)}{support(X, D)}$ . A class association rule (CAR) is an association rule where the head or consequent of the rule refers to the class attribute.

Different implementations of associative classifiers use different association rule mining techniques. For example, the Apriori algorithm [2] is used by CBA [16], ARC-AC [4], ARC-BC [4], ACRI [22] and ARUBAS [9], while CMAR [15] uses the FP-tree algorithm [13], CPAR [27] uses the FOIL algorithm [21] and CorClass [29] uses the Morishita & Sese Framework [19].

Class association rules can be generated from a single data set containing all training transactions, which is e.g. the case for ARC-AC, CMAR or CBA, or can be generated from a set of data sets, where training cases are grouped per class label. The latter is the case for ARC-BC and makes it more probable for small classes to have representative class association rules. Furthermore, all association rule mining algorithms produce the same set of class association rules, but differ in terms of computational complexity. One exception is the FOIL algorithm used in the CMAR implementation, which is a heuristic rather than an exact solution and only gives an approximation of the exhaustive set of class association rules meeting specific support and confidence criteria.

**2.2. Pruning.** Once the CARs are generated from the training set, most associative classifiers apply some pruning strategy to reduce the size of the rule set. Even if there is no separate post-pruning step, all algorithms apply some sort of pre-pruning during the rule generation step by setting a support and/or confidence threshold. This pre-pruning technique is an isolated pruning technique as the CARs are evaluated individually, in isolation from the other CARs. Other isolated pruning techniques are Pessimistic Error Pruning (PEP) and Correlation Pruning (CorP). Pessimistic Error Pruning (PEP), applied in CBA [16], uses the

pessimistic error rate from C4.5 [21] to prune, while Correlation Pruning (CorP), which is applied in CMAR [15], uses the correlation between the rule's body and the rule's head.

Some associative classifiers use non-isolated pruning techniques which take multiple rules into account when deciding whether or not to prune a specific rule. A well known non-isolated pruning technique is the Data Coverage Pruning technique (DCP), which is applied in CBA [16], ARC-AC [4], ARC-BC [4] and CMAR [15]. DCP consists of two steps. First, the rule set is ordered according to confidence, support and rule size. Rules with the highest confidence go first. In case of a tie, rules with the highest support take precedence. In case of a tie in terms of confidence and support, the smaller the rule, i.e. the more general a rule is, the higher the ranking. Once the rule set is ordered, the rules are taken one by one from the ordered rule set and are added to the final rule set until every record in the training set is matched at least  $\alpha$  times. For CBA, ARC-AC and ARC-BC this parameter  $\alpha$  is fixed to 1, while in CMAR  $\alpha$  is a parameter which needs to be set by the user. Confidence Pruning (ConfP) is another non-isolated pruning technique which is used by CMAR, ARC-AC, ARC-BC. ConfP prunes all rules which are generalized by another rule with a higher confidence level.

**2.3. Classification.** Once the CARs are generated and pruned, the associative classifier uses all these pieces of local knowledge to classify new instances. While some associative classifiers apply order-based classification, others use non-order-based classification. With order-based classification, the association rules are ordered according to a specific criterion, while non-order-based classifiers do not rely on the order of the rules.

Among the order-based classification schemes, the Single Rule Classification approach has to be distinguished from the Multiple Rule Classification approach. The former approach orders the rules and uses the first rule which covers the new instance to make a prediction. The predicted class is the selected rule's head. This classification scheme is used by CBA, CorClass and ACRI. CBA and CorClass order the rules according to confidence, support and rule size in the same way the data coverage pruning technique does. ACRI on the other hand, allows the users to select from four different ordering criteria, i.e. a cosine measure, the support, the confidence or the coverage.

Multiple Rule Classification, which is used by CPAR, selects those rules which cover the new instance, groups them per class and orders them according to a specific criterion. Finally, a combined measure is calculated for the best Z rules, where Z is a user-defined parameter. With CPAR, the rank of each rule is determined by the expected accuracy of the rule.

Furthermore, some associative classifiers, such as CMAR, ARC-AC, ARC-BC and CorClass, use a non-order-based classification scheme. These classification schemes select the rules which cover the new instance, group them per class and calculate a combined measure per class value. This approach is almost identical to the order-based multiple rule classification scheme, except for the ordering step.

**3.** Classifier PGN. This section introduces the implementation details of our new associative classifier PGN. The main idea behind this associative classifier is to break with the existing habit of putting the primary focus on support when generating association rules. Instead, PGN focuses primarily on confidence, using only 100% confidence rules to classify with. The structure of the PGN classifier follows the general three-step structure of most associative classifiers, discussed in the previous section. Next, each of these three steps will be discussed in detail, preceded by a subsection introducing the necessary notation and definitions.

**3.1. Notation.** Association rule mining traditionally deals with transactional data, which differs structurally from rectangular data, which is more common in the domain of classification techniques. A record in a transactional data set is represented as a set of items, e.g.  $X_1 = \{a, b, d, e\}$ , while the same record in a rectangular data set is represented as a set of attribute-value pairs, e.g.  $X_1 = \{\langle a, 1 \rangle, \langle b, 1 \rangle, \langle c, 0 \rangle, \langle d, 1 \rangle, \langle e, 1 \rangle\}$ . The most striking difference between both types of data sets is that the size of an instance in a transactional database is not fixed, while it is in a rectangular data set. Furthermore, the concept of a class attribute, i.e. the attribute whose value the classification algorithm tries to predict, is not easily represented in a transactional context. Therefore, this section introduces some new notation which allows us to define association rule mining concepts in the context of rectangular data.

In a rectangular data set D, each instance  $X_i = \{a_1^i, \ldots, a_j^i, \ldots, a_J^i, \}$ consists of a set of J attribute-value pairs  $a_j^i = \langle a_j, x_j^i \rangle$  where  $x_j^i$  represents the value of attribute  $a_j$  for instance  $X_i$ . The attributes are assumed to be nominal or categorical, and thus  $x_j^i \in \{-, 1, 2, \ldots, K^j\}$  with "-" representing "arbitrary" value. Furthermore, one of the attributes represents the class to which the instance belongs. To distinguish the class attribute from the other attributes, the corresponding attribute-value pair will be denoted as  $a_C^i = \langle a_C, c^i \rangle$ . Often, a simplified notation is used by representing a record as a set of attribute values, which results in the following notation:  $X_i = \{x_1^i, \ldots, x_{J-1}^i, c^i\}$ . Note that each record represents a class association rule and every class association rule can be expressed using the same notation as for records. For example, the association rule  $R_l : \{x_1^l, \ldots, x_{J-1}^l\} \Rightarrow \{c^l\}$  corresponds with notation  $R_l = \{x_1^l, \ldots, x_{J-1}^l, c^l\}$  and vice versa. Attributes which are not part of an association rule are denoted with a 'missing value', e.g the rule  $R_l : a_1 = 1 \land a_3 = 2 \Rightarrow a_C = 1$  is represented as  $R_l = \{\langle a_1, 1 \rangle, \langle a_2, - \rangle, \langle a_3, 2 \rangle, \langle a_C, 1 \rangle\}$ .

Before support and confidence can be defined, two new relationships between a rule  $R_l$  and a record  $X_i$  need to be defined.

**Definition 1: Covering relation** " $\subset$ ". A rule  $R_l = \{x_1^l, \ldots, x_{J-1}^l, c^l\}$ covers a record  $X_i = \{x_1^i, \ldots, x_{J-1}^i, c^i\}$  if the rule's antecedent corresponds with the record, that is:

$$R_l \subset X_i \Leftrightarrow \forall x_j^l | 1 \le j \le J - 1, x_j^l \ne -\} : x_j^l = x_j^i$$

**Definition 2: Matching relation** " $\subseteq$ ". A rule  $R_l = \{x_1^l, \ldots, x_{J-1}^l, c^l\}$ matches a record  $X_i = \{x_1^i, \ldots, x_{J-1}^i, c^i\}$  if both the rule's antecedent and consequent corresponds with the record, that is:

$$R_l \subseteq X_i \Leftrightarrow R_l \subset X_i \text{ and } c^l = c^i$$

Now the support and confidence of a rule can be defined with the new notation:

**Definition 3: Support.** 

$$support(R_l, D) = |\{X_i \in D | R_l \subseteq X_i\}|$$

Definition 4: Confidence.

$$confidence(R_l, D) = \frac{|\{X_i \in D | R_l \subseteq X_i\}|}{|\{X_i \in D | R_l \subset X_i\}|}$$

**3.2.** Association Rule Mining. To illustrate the algorithm, a simple data set shown in Table 1 is used as example.

Since the primary focus of the classifier PGN is on the rule's confidence, we cannot use the downward closure property of the support metric to limit the search space of confident association rules. The downward closure property specifies that by making an association rule more specific, i.e. adding additional antecedents, the support can not increase. The Apriori algorithm exploits this property by starting from very general rules and making them incrementally more specific until supports drops below a specified threshold. However, specifying such threshold will possible prevent us from learning all 100% confidence rules, which violates the goal of PGN.

Table 1. Example data set. The final attribute is the class attribute

Records	
$X_1 = \{1, 2, 4, 1, 1\}$	
$X_2 = \{1, 2, 3, 1, 1\}$	
$X_3 = \{3, 1, 3, 2, 1\}$	
$X_4 = \{3, 1, 4, 2, 1\}$	
$X_5 = \{1, 2, 4, 1, 1\}$	Equal to $X_1$
$X_6 = \{3, 1, 4, 2, 1\}$	Equal to $X_4$
$X_7 = \{3, 1, 1, 2, 2\}$	
$X_8 = \{2, 1, 1, 2, 2\}$	
$X_9 = \{3, 1, 2, 2, 2\}$	

PGN starts by adding all records to the set of association rules. For each class, a separate set of association rule is generated. In our example, the first four records are added as rules for class 1. Records  $X_5$  and  $X_6$  correspond to  $X_1$  and  $X_4$  respectively and are therefore not added since this would only result in duplicate rules. The final three records are added to the rule set for class 2. This is illustrated in Figure 1.

Class 1				Class 2		
$\bigcirc$	$\bigcirc$	$\bigcirc$	$\bigcirc$	•		
R <sub>1</sub> ={1,2,4,1, <b>1</b> }	R <sub>2</sub> ={1,2,3,1,1}	R <sub>3</sub> ={3,1,3,2, <b>1</b> }	R <sub>4</sub> ={3,1,4,2,1}	R <sub>5</sub> ={3,1,1,2, <b>2</b> }	R <sub>6</sub> ={2,1,1,2, <b>2</b> }	R <sub>7</sub> ={3,1,2,2, <b>2</b> }
X,,X <sub>5</sub> }	{X <sub>2</sub> }	{X <sub>3</sub> }	{X <sub>4</sub> ,X <sub>6</sub> }	{X <sub>7</sub> }	{X <sub>8</sub> }	{X_}}

Fig. 1. Adding records to the appropriate rule set

Next for each class, the intersection of every pair of rules is taken (cf. Definition 5). If the intersection results in a new rule which is not present in the rule set, it is added. This process continues until no more intersections are possible. The result of this step for the example data set is shown in Figure 2.

**Definition 5: Intersection** " $\cap$ ".  $R_1 \cap R_2 = R_3$  such that  $\forall x_j^3 \in R_3$  it holds that  $x_j^3 = \begin{cases} x_j^1 & \text{if } x_j^1 = x_j^2 \\ - & \text{if } x_j^1 \neq x_j^2 \end{cases}$ 

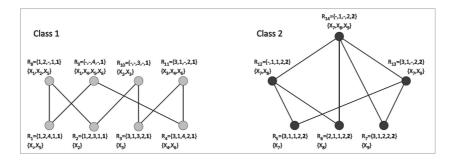


Fig. 2. Creating new association rules through intersection

**3.3. Pruning.** In the pruning stage of PGN, association rules are removed from the rule set in two steps.

Firstly, all rules with a confidence less than 100% are removed, and secondly rules for which a more general version is present in the rule set are also pruned. Pruning for confidence is performed in accordance with Definition 6. Application of this pruning step is illustrated in Figure 3. After all comparisons between rules from different classes are made, all rules marked for removal are pruned.

Definition 6: Pruning for confidence.

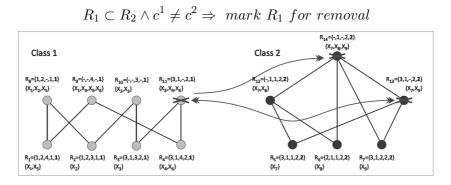


Fig. 3. Pruning for confidence

It can easily be proven that pruning for confidence results in association rules with confidence equal to 100%.

# Proof. Pruning for confidence removes rules with confidence less than 100%.

Assume that  $R_1 \subset R_2$  and  $c^1 \neq c^2$ . Since every rule is either a record from data set D or an intersection between two rules, we know that the support of every rule is at least 1. From this follows that a record  $X_i$  exists such that  $R_2 \subseteq X_i$ . Given that  $R_1 \subset R_2$ , it follows that  $R_1 \subset X_i$ . However, since  $R_2 \subseteq X_i$  and  $c^1 \neq c^2$ , we know that  $R_1 \subseteq X_i$  cannot hold and  $confidence(R_1, D) < 1$ .

After all rules with a confidence level less than 100% are removed, a second pruning step is performed which retains only the most general rules. Pruning for general rules is performed as detailed in Definition 7. Application of this pruning step is illustrated in Figure 4. After all pairs of rules within each class are compared, all rules marked for removal are pruned.

## Definition 7: Pruning for general rules.

 $R_1 \subset R_2 \wedge c^1 = c^2 \Rightarrow mark \ R_2 \ for \ removal$ 

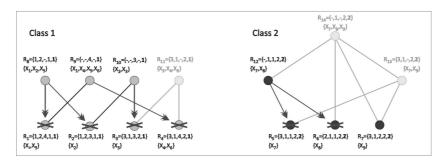


Fig. 4. Pruning for general rules

As a result of these two pruning steps, only general and highly confident rules are retained. For the example data set, the rules in Table 2 were retrieved after pruning.

Rule	Support	Support set
$R_1 = \{1, 2, -, 1, 1\}$	3	$\{X_1, X_2, X_5\}$
$R_2 = \{-, -, 4, -, 1\}$	4	$\{X_1, X_4, X_5, X_6\}$
$R_3 = \{-, -, 3, -, 1\}$	2	$\{X_2, X_3\}$
$X_9 = \{3, 1, 2, 2, 2\}$	1	$\{X_9\}$
$R_5 = \{-, 1, 1, 2, 2\}$	2	$\{X_7, X_8\}$

Table 2. Association rules after pruning

**3.4. Classification.** To classify new instances with the pruned rule set, the definition for the size of an association rule must be introduced first. The association rule size corresponds to the number of non-class attributes which have a non-missing value.

Definition 8: Association Rule Size.

$$|R_l| = \left| \left\{ x_j^l | 1 \le j \le J - 1, x_j^l \ne - \right\} \right|$$

This allows us to define an intersection percentage between a record  $X_i$ and an association rule  $R_l$ :

#### **Definition 9: Intersection Percentage.**

$$IP(X_i, R_l) = 100 * \frac{|X_i \cap R_l|}{R_l}$$

To classify a new instance, the intersection percentage between the test case and every rule is calculated. This allows for three different scenarios:

- When the maximum intersection percentage occurs only once for one single rule, the class of this rule becomes the predicted class for the new instance.
- When the maximum intersection percentage occurs multiple times, but only for rules from the same class, the class of these rules becomes the predicted class for the new instance.
- When the maximum intersection percentage occurs multiple times for rules from different classes, the supports of these rules are summed per class. The class with the highest aggregated support becomes the predicted class for the new instance.

Note that this classification scheme also uses association rules which do not cover the test case perfectly for classification purposes.

Let's illustrate this classification method with the pruned rule sets in Table 2. Assume a new instance  $X_i = \{1, 2, 1, 2, ?\}$  which needs to be classified ("?" marks the unknown value of the class label). Firstly, the intersection percentage between  $X_i$  and every rule is calculated and shown in Table 3. The maximum intersection percentage is 0.667 and occurs for rules  $R_1$  and  $R_5$  which belong to different classes. Considering only the rules with an intersection percentage of 0.667, the summed support for class 1 is 3 and the summed support for class 2 is 2. Consequently, the new instance is predicted to belong to class 1.

$R_l$	$X_i \cap R_l$	$IP(X_i, R_l)$	Support
$R_1 = \{1, 2, -, 1, 1\}$	$\{1, 2, -, -, ?\}$	0.667	3
$R_2 = \{-, -, 4, -, 1\}$	$\{-, -, -, -, ?\}$	0	4
$R_3 = \{-, -, 3, -, 1\}$	$\{-, -, -, -, ?\}$	0	2
$R_4 = \{3, 1, 2, 2, 2\}$	$\{-, -, -, 2, ?\}$	0.250	1
$R_5 = \{-, 1, 1, 2, 2\}$	$\{-, -, 1, 2, ?\}$	0.667	2

Table 3. Classification of  $X_i = \{1, 2, 1, 2, ?\}$ 

4. Empirical Analysis. The goal of this section is to empirically analyze the performance of PGN.

The experiments were performed on various data sets from the UCI Machine Learning Repository [11]. The used data sets are described in Table 4. Data sets containing continuous attributes were discretized first by means of the Chi-merge method [14]. This discretization method is based on the  $\chi^2$  statistic and uses a Chi-square threshold as stopping rule. In our experiments, the Chi-square threshold was set to 95%.

Data set	# attributes	# classes	# instances	Attribute type
annealing	38	5	798	Categorical, Integer, Real
audiology	69	24	200	Categorical
balance scale	4	3	624	Categorical
breast cancer wo	9	2	699	Categorical
car	6	4	1728	Categorical
cmc	9	3	1473	Categorical, Integer
credit	15	2	690	Categorical, Integer, Real
ecoli	7	8	336	Real
forestfires	12	2	517	Real
glass	9	6	214	Real
hayes-roth	4	3	132	Categorical
hepatitis	19	2	155	Categorical, Integer, Real
iris	4	3	150	Real
lenses	4	3	24	Categorical

$\operatorname{mammographic}$	5	<b>2</b>	961	Integer
monks1	6	2	432	Categorical
monks2	6	2	601	Categorical
monks3	6	2	554	Categorical
soybean	35	19	307	Categorical
tae	5	3	151	Categorical, Integer
tic tac toe	9	2	958	Categorical
votes	15	2	435	Categorical
wine	13	3	178	Integer, Real
winequality-red	11	6	1599	Real
ZOO	16	7	101	Categorical, Integer

The goal of the experiments is to compare PGN against other classifiers and to find significant differences between the classifiers in terms of accuracy. For these purposes the methodology suggested by Demšar [8] is followed. First, unbiased estimates of the classifiers' accuracies will be estimated by means of a five-fold cross validation for the observed datasets. Next, the Friedman test is used to detect statistically significant differences between the classifiers in terms of average accuracy. The Friedman test is a non-parametric equivalent of the repeated-measures ANOVA test, but is based on the ranking of the algorithms for each data set instead of the true accuracy estimates. In his paper, Demšar discusses several reasons why the ANOVA test is inappropriate for comparing multiple classifiers and why analyses should be performed on the ranking information instead of the overall accuracies. The interested reader is referred to [8]. If according to the Friedman test, differences between the classifiers exist, we use the Nemenyi test to compare each classifier with all other classifiers. The Nemenyi test controls for family-wise error in multiple hypothesis testing and is similar to the Tukey test for ANOVA. The results of the Nemenyi test are shown by means of critical difference diagrams.

The classifiers to compare with are representatives of different classification schemes, as follows:

 Associative classifiers: PGN and CMAR (using support threshold 1% and confidence threshold 50%);

- Decision Rules: One R, JRip (pruned and unpruned), Decision Table; NNge;
- Decision Trees: REP Tree, J48 (pruned and unpruned), LAD Tree;
- Nearest Neighbor learners: IBk, KStar;
- Bayes: Naïve Bayes, Bayes Net, HNB, WAODE, LBR;
- Ensemble methods (Bagging): Random Forest;
- Support Vector Machines: SMO;
- Neural Networks: Multilayer Perceptron.

Experiments were made using the following programs:

- program realization of PGN in data mining environment PaGaNe [18];
- the program realization of CMAR in the LUCS-KDD Repository (http://www.csc.liv.ac.uk/~frans/KDD/);
- for all other classifiers their Weka implementation are used [26].

All classifiers received the discretized data set to begin with.

Table 5 shows the average accuracies of five-fold cross validation for examined classifiers over chosen datasets.

Table 5a. Average accuracies of five-fold cross validation (first 11 classifiers)

classifier	$\operatorname{PGN}$	CMAR	One R	JRip-	Dec.	JRip-	NNge	REP	J48-	J48-	LAD
dataset				unpr.	Table	pruned		Tree	pruned	unpr.	Tree
annealing	96.24	95.99	83.71	99.00	98.37	98.12	97.24	97.62	98.12	98.75	98.12
audiology	75.50	59.18	47.00	68.50	61.00	69.50	67.00	62.50	72.00	72.00	71.50
$balance\_scale$	77.89	86.70	60.10	72.76	66.83	71.95	70.68	67.15	66.18	69.87	82.69
$breast\_cancer\_wo$	96.43	93.85	91.85	92.85	92.42	93.28	94.99	93.99	94.28	94.71	94.85
car	92.59	81.77	70.03	87.44	91.43	86.75	94.33	88.2	90.8	93.17	90.45
cmc	49.90	53.16	47.25	45.55	49.42	50.38	44.81	50.17	51.60	48.07	54.86
credit	87.54	87.10	85.51	81.45	85.8	85.07	80.14	85.07	85.36	83.91	86.67
ecoli	79.76	81.26	60.42	75.91	76.50	80.07	77.70	79.17	77.09	78.28	81.27

forestfires	57.63	58.80	53.38	55.31	52.03	54.76	54.36 $53.95$	53.96	52.41 $57.26$
glass	78.51	78.04	54.67	71.98	61.23	66.40	$71.53 \ 67.29$	73.38	74.76 $71.95$
hayes-roth	81.94	83.42	50.77	78.86	51.51	78.12	75.10 73.53	68.23	$69.00 \ 87.24$
hepatitis	80.65	84.52	81.94	76.78	82.58	77.42	81.29 79.36	79.36	77.42 $77.42$
iris	92.67	92.67	94.67	93.33	92.67	92.67	$94.67 \ 93.33$	94.67	93.33 93.33
lenses	74.00	88.00	62.00	87.00	92.00	83.00	70.00 80.00	83.00	$75.00 \ 83.00$
$\operatorname{mammographic}$	80.75	82.11	82.00	78.98	82.73	81.69	$76.28 \ 81.69$	81.69	$83.46 \ 80.96$
monks1	100.00	100.00	74.98	99.31	100.00	87.53	$96.05 \ 88.91$	94.68	$93.28 \ 80.08$
monks2	73.06	59.74	65.73	58.74	64.40	58.73	73.87 63.90	59.90	60.91 $68.39$
monks3	98.56	98.92	79.97	98.56	98.92	98.92	98.20 98.92	98.92	98.92 $98.92$
soybean	93.15	78.48	37.44	87.28	75.24	85.35	$89.24\ 78.18$	87.64	$87.95\ 77.85$
tae	52.94	35.74	45.76	33.72	47.70	34.43	$50.88 \ 40.43$	46.97	$47.61\ \ 45.64$
tic_tac_toe	88.93	98.75	69.93	97.29	73.70	98.02	$86.53 \ 80.37$	84.23	84.23 73.70
votes	95.86	94.02	95.63	94.25	93.79	94.71	$94.71 \ 95.40$	95.17	94.25 $95.63$
wine	96.09	91.70	78.63	89.33	80.90	90.45	$92.18\ 88.16$	87.03	88.19 90.98
winequality-red	64.98	56.29	55.54	48.65	55.97	53.72	60.79 $57.03$	58.22	$59.16\ 56.41$
ZOO	98.10	94.19	73.29	90.14	88.19	88.19	$95.14\ 82.19$	94.14	$95.14 \ 98.10$

Table 5b. Average accuracies of five-fold cross validation (next 10 classifiers)

classifier	IBk	KStar	Naïve	Bayes	HNB	WAO	LBR	Rand.	$\operatorname{SMO}$	Mult.
dataset			Bayes	Net		DE		Forest		perc.
annealing	98.25	98.75	91.61	91.11	97.62	96.99	96.87	97.62	99.12	99.12
audiology	76.50	76.00	64.50	71.00	68.00	71.50	65.00	73.50	76.50	78.50
balance_scale	85.26	86.70	90.54	90.54	87.02	88.14	90.54	75.48	89.42	98.72
breast_cancer_wo	95.85	95.28	97.14	97.14	95.13	95.85	97.14	95.42	95.99	96.28
car	92.94	86.81	85.19	85.30	92.24	90.11	91.95	93.52	92.59	99.83
cmc	47.12	50.31	50.45	50.31	52.96	52.68	52.55	48.68	53.50	47.73
credit	82.90	84.78	86.38	86.38	84.93	85.94	86.23	85.51	85.94	86.09
ecoli	79.76	80.36	84.84	84.54	79.77	82.75	84.84	80.36	84.24	80.67
forestfires	56.69	56.68	58.02	58.21	56.29	60.73	58.02	58.42	61.11	58.01

glass	78.98	78.99	74.33	74.34	75.70	77.13	74.33	76.19	77.12	74.32
hayes-roth	63.67	61.40	85.67	85.67	72.82	76.61	85.67	76.61	83.39	83.45
hepatitis	81.29	80.65	86.45	85.16	85.81	83.87	87.10	83.23	77.42	81.29
iris	93.33	93.33	92.67	92.67	92.00	93.33	92.67	94.67	93.33	94.67
lenses	78.00	78.00	70.00	70.00	54.00	70.00	70.00	74.00	70.00	74.00
mammographic	80.44	81.17	82.62	82.42	82.42	82.94	82.42	81.90	81.48	80.44
monks1	97.92	97.92	74.98	74.98	100.00	74.29	100.00	96.30	74.98	100.00
monks2	71.55	76.88	61.41	61.24	67.90	63.73	66.57	65.39	65.73	100.00
monks3	97.66	97.84	96.39	96.39	98.38	98.56	98.74	98.02	96.75	98.92
soybean	90.87	91.85	82.76	86.33	91.85	90.87	86.99	89.91	90.87	92.18
tae	57.53	55.57	46.99	46.34	52.93	53.59	50.30	48.92	51.61	54.92
tic_tac_toe	97.39	95.30	71.29	71.40	77.03	73.27	84.97	91.13	98.33	97.81
votes	93.79	93.56	89.89	89.89	94.48	95.40	94.02	95.63	95.86	95.40
wine	96.11	96.11	98.89	99.44	98.33	97.20	98.89	94.40	98.33	97.76
winequality-red	64.29	64.67	58.60	58.47	62.29	61.91	59.28	64.35	59.04	64.04
Z00	96.14	96.14	94.10	96.10	97.10	98.05	94.10	96.10	98.05	96.14

Table 6 shows the ranks of these classifiers over the data sets. Let's mention that if two or more classifiers have equal accuracies, they share corresponded average ranks.

Table 7 shows the average rank for each classifier over the 25 UCI data sets. The Friedman test has a  $\chi^2$  value of 95.579 with 20 degrees of freedom. For this degree of freedom the null hypothesis critical value is  $\alpha_{0.10} = 28.412$ . This indicates that there are statistically significant differences in accuracy among these 21 classifiers.

The rejecting of null-hypothesis of Friedman test gives the assurance to make post-hoc Nemenyi test. Figure 5 shows the results of the Nemenyi test.  $CD_{0.10}$  shows the groups of classifiers that are not significantly different at p=0.1. From these results we see that PGN is competitive with techniques such as Neural Networks (Multilayer Perceptron), Support Vector Machines (SMO), Ensemble methods (Random Forest) and Bayes techniques and statistically outperforms more of the representatives of Decision Trees and Decision Rules.

τ	Mult.perceptror	1.5	1	1	ъ	1	17	7	$\infty$	$\infty$	13	5 L	11	n	12	18.5	3.5	1	4.5	2	co	4	2	9	5 L	2
	OWS	1.5	2.5	5	9	6.5	7	8.5	4	1	9	7	18.5	9.5	16.5	14	18.5	9.5	18	9	4	7	1.5	4.5	11	3.5
	RandForest	12	9	13	6	က	15	11.5	9.5	4	2	11.5	4	ი	12	10	10	11	15	x	10	x	4	11	က	9.5
	гвя	16	16	ŝ	7	6	9	9	1.5	6.5	11.5	ŝ	1	17	16.5	9	3.5	$\infty$	6	13	6	11	15.5	2.5	6	15.5
	MYODE	15	9.5	9	7.5	13	5	8.5	5	2	5	11.5	9	9.5	16.5	2	21	14	11	9	4	18	7	4	4	3.5
	HNB	12	14	2	11	$\infty$	4	16	12	13	$\infty$	15	ŝ	21	21	9	3.5	4	13	3.5	9	15	12	4.5	9	r.
	təVesVet	20	11	3	10	18	10.5	4.5	3	5	10	3	4	17	16.5	9	18.5	16	19.5	14	15	19	20.5	1	13	9.5
$\operatorname{sets}$	səysBəvisN		17																							
data	X Star	4.5	4	8.5	10	16	10.5	17	9.5	12	Ч	19	13.5	9.5	8.5	15	8.5	2	16	3.5	2	2	19	8.5	7	2
The ranks of classifiers over the data	भ धा		2.5																							
s ove	ээтГДАЛ		9.5																							
sifier	b9nrnqnu-84€		7.5																							
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	CMAR	18	20	×.	17	20	c,			S					2			19	4.5	17	19	1	15.	13	17	13
	ЬСИ	17	5	12	4	6.5	13	1	13.5	6	ŝ	x	13.5	17	12	17	3.5	4	11	1	5	6	1.5	10	1	1.5
	classifier dataset	annealing	audiology	balance_scale	breast_canc.	car	cmc	credit	ecoli	forestfires	glass	hayes-roth	hepatitis	iris	lenses	mammogr.	monks1	monks2	monks3	$\operatorname{soybean}$	tae	tic_tac_toe	votes	wine	wineqred	200

Table 7 Average ra	nks on 25 UCL	data sets for PGN	and 20 other classifiers

	PGN	CMAR	One F	R JRip-	- Dec	. JRi	p- N	Nge	REP	J48-	J48-	LAD
_				unpr.	. Tabl	le prui	ned		Tree	pruned	unpr.	Tree
Avg.Rank	7.96	10.52	17.18	14.40	13.9	4 13.	78 1	2.50	14.20	12.48	12.08	10.20
	IB k	K Star	Naïve Bayes	Bayes Net	HNB	WAO DE	LBR	Rano Fores		IO Mul <sup>a</sup> perc		
Avg.Rank	9.66	9.36	11.48	11.18	9.86	8.82	8.68	8.92	2 7.6	6.20	)	
SMO PGN LBR WAOE Rando K Star IB k HNB	2 J yer Perc E m Fores					9 10			3 14		Rip-unpru REP ecision Tr JRip-pru	Tree able ned Nge ned

Fig. 5. Comparison PGN and 20 other classifiers (Nemenyi test)

Finally, note that in contrast with the some other classifiers (especially associative classifiers), PGN is a parameter free classifier.

5. Conclusions. The goal of this article is to question the supportfirst principle used by many associative classifiers when mining for association rules. Instead, a new associative classifier, called PGN, was developed which turns the common approach around and focuses primarily on the confidence of the association rules and only in a later stage on the support of the rules. The main purpose of this research was to provide a proof of concept for this new approach and collect evidence about its potential.

The experimental results are very positive and show that PGN is competitive with some of the more advanced classification methods such as Neural Networks, Support Vector Machines, Ensemble methods and Bayes techniques, while statistically outperforming more of the representatives of Decision Trees and Decision Rules. At the same time, PGN has the advantage over the other Associative Classifiers that it is parameter free.

In general, the results provide evidence that the confidence-first approach yields interesting opportunities.

Now that the proof of concept is given, future research must focus on the computational efficiency of the algorithm, since this was not the focus during this research. Particularly, the association rule mining step is computationally expensive in the current implementations. Another interesting direction for future research concerns an adjustment of the current algorithm which to mine for highly confident association rules which are not necessarily 100% confidence results.

### $\mathbf{R} \, \mathbf{E} \, \mathbf{F} \, \mathbf{E} \, \mathbf{R} \, \mathbf{E} \, \mathbf{N} \, \mathbf{C} \, \mathbf{E} \, \mathbf{S}$

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