

# The program Equivalence in the software package QextNewEdition

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# Definitions

Two linear  $q$ -ary codes  $C_1$  and  $C_2$  are said to be *equivalent* if the codewords of  $C_2$  can be obtained from the codewords of  $C_1$  via a sequence of transformations of the following types:

1. permutation of coordinates;
2. multiplication of the elements in a given coordinate by a nonzero element of  $F_q$ ;
3. application of a field automorphism to the elements in all coordinates simultaneously.

An automorphism of a linear code  $C$  is a sequence of such transformations that maps each codeword of  $C$  onto a codeword of  $C$ . The automorphisms of a code  $C$  form a group, called the automorphism group of the code and denoted by  $\text{Aut}(C)$ .

# Definitions

A canonical representative map for this action is a function

$\rho : \Omega \rightarrow \Omega$  that satisfies the following two properties:

(1) for all  $X \in \Omega$  it holds that  $\rho(X) \sim X$ ;

(2) for all  $X, Y \in \Omega$  it holds that  $X \sim Y$  implies  $\rho(X) = \rho(Y)$ .

# Definitions

Denition 3. Two matrices of the same size are isomorphic if the rows of the second one can be obtained from the rows of the rst one by a permutation of the columns.

This denition is based on the natural action of the symmetric group  $S_n$  on the set of columns.

Any permutation of the columns of  $A$  which maps the rows of  $A$  into rows of the same matrix, is called an automorphism of  $A$ . The set of all automorphisms of  $A$  is a subgroup of the symmetric group  $S_n$  and we denote it by  $\text{Aut}(A)$ .

# History

1. B.D. McKay. Practical graph isomorphism. *Congressus Numerantium*, 30: 1981
2. J. Leon, Computing automorphism groups of error-correcting codes, *IEEE Trans, Info. Theory* 28 (1982),
3. Ст. Капралов. Алгоритми за генериране и изследване на орбитни матрици. 100 години от рождението на академик Любомир Чакалов, Трудове на юбилейна научна сесия, Самоков, 14–15.02.1986, 114–121.

# What is new?

Generating set

Alocation of dinamic nemory

Range - for  $GF(q)$   $q < 64$ :  $q$  prime and  $q=4$

Binary representation of generating set of codewords

# Experimental results

Parameters	Time in secinds	parameters	Time in seconds
[100,50]_2	2.8	[36,10]_2	0.0005
[90,30]_2	0.07	[36,10]_3	0.021
[90,30]_3	75.44	[36,10]_7	0.025
[1000,10]_4	0.5	[36,10]_17	6.759
[1000,12]_4	2.31	[30,10]_41 [36,10]_41	32.11 2119.75

Program 'Equivalence' from QextNewEdition VER: 0.1

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Input file: RES\_DIR0\EXAM Output file RES\_DIR0\EXAM\_r

1. Calculate inequivalent codes
2. Calculate inequivalent matrices
3. What to print in the output file for codes
4. What to print in the output file for matrices
5. Change the name of the input file
6. Random codes - write in file with name 'RES\_DIR0//EXAM.'
7. Random codes with automorphism - write in file with name 'RES\_DIR0//EXAM.'
8. About QextNewEdition
9. Exit

Choose:

What to print in the output file?

- yes 1. Generator matrix
  - 2. Rank of the matrix
  - 3. Systematic coordinates
  - 4. Matrices with different systematic coordinates
  - 5. Minimum distance
  - 6. Spectrum (or partial spectrum)
  - 7. Generating set of codewords
  - yes 8. Order of automorphism group AUT
  - 9. Generators of AUT by coordinates
  - 10. Coordinates' orbits
  - 11. Additional information
  - yes 12. Elapsed time
  - 13. Noting
  - 14. All options
  - 15. Start
  - 16. Exit
- Choose:

What to print in the output file for matrices?

yes 1. Matrix

yes 2. Order of automorphism group AUT

3. Generators of AUT by columns

4. Generators of AUT by rows

5. Orbits of columns

6. Orbits of rows

7. Additional information

yes 8. Elapsed time

9. Noting

10. All options

11. Start

12. Exit

Choose:

```
D:\MDSpg06.11.2020\RES_DIR\EXAM_r - Notepad++
File Edit Search View Encoding Language Settings Tools Macro Run Plugins Window ?
RES x EXAM x TABLE2.TTT x exam_m x exam11_r x EXAM_r x
1
2 ? 10 30 2 1 1
3 100000000001110011001001100111
4 010000000000111001101100110011
5 001000000000011100111110011001
6 000100000010001110011111001100
7 000010000011000111000111100110
8 000001000001100011100011110011
9 000000100000110001111001111001
10 000000010010011000111100111100
11 000000001011001100010110011110
12 000000000111100110000011001111
13 k= 10
14 d= 8
15
16 Weight spectrum:
17 8^5 10^80 12^175 14^200 16^310 18^200 20^53 |AUT|= 10 TRANS 0
18 =====
19 |AUT|= 10 Generator of |AUT|
20 - 1 (10,1,2,3,4,5,6,7,8,9) (20,11,12,13,14,15,16,17,18,19) (30,21,22,23,24,25,26,27,28,29) =====
21
22 3 ORBITS by column
23 { 1, 10, 9, 8, 7, 6, 5, 4, 3, 2, }, { 11, 20, 19, 18, 17, 16, 15, 14, 13, 12, }, { 21, 30, 29, 28, 27, 26, 25, 24, 23, 22, },
24
25 == Elapsed time: 0.00s
26
27 ? 10 30 2 2 2
28 100000000001000100101110000010
29 010000000000100010010111000001
30 001000000010010001001011100000
31 000100000010010001001011100000
32 000010000001001000100101110000
33 000001000010010010000001011100
34 000000100001001001000000101110
35 000000010000100100100000010111
36 000000001000010010011000001011
37 000000000110001001001100000101
38 k= 10
39 d= 8
40
41 Weight spectrum:
42 8^10 10^50 12^170 14^280 16^305 18^130 20^58 22^20 |AUT|= 10 TRANS 0
43 =====
44 |AUT|= 10 Generator of |AUT|
45 - 1 (10,1,2,3,4,5,6,7,8,9) (20,11,12,13,14,15,16,17,18,19) (30,21,22,23,24,25,26,27,28,29) =====
Normal text file length: 694 464 lines: 17 396 Ln: 1 365 Col: 58 Pos: 47 231 Windows (CR LF) UTF-8 INS
```

```

1580 000000001000010100100110011110
1581 000000000100001010010011001111
1582 k= 10
1583 d= 8
1584
1585 Weight spectrum:
1586 8^15 10^40 12^165 14^300 16^300 18^120 20^63 22^20 |AUT|= 10 TRANS 0
1587 =====
1588 |AUT|= 10 Generator of |AUT|
1589 - 1 (10,1,2,3,4,5,6,7,8,9) (20,11,12,13,14,15,16,17,18,19) (30,21,22,23,24,25,26,27,28,29) =====
1590
1591 3 ORBITS by column
1592 { 1, 10, 9, 8, 7, 6, 5, 4, 3, 2, }, { 11, 20, 19, 18, 17, 16, 15, 14, 13, 12, }, { 21, 30, 29, 28, 27, 26, 25, 24, 23, 22, },
1593
1594 == Elapsed time: 0.00s
1595
1596 67 from input file equivalent to ->> 37 from output file TR -0
1597 PERM COL
1598 1 -> 11 ; 2 -> 14 ; 3 -> 17 ; 4 -> 20 ; 5 -> 13 ; 6 -> 16 ; 7 -> 19 ; 8 -> 12 ; 9 -> 15 ; 10 -> 18 ; 11 -> 1 ; 12 -> 4 ; 13 -> 7 ; 14 -> 10 ; 15 -> 3 ; 16 -> 6 ; 1
1599
1600 ? 10 30 2 63 68
1601 100000000010010111111100000001
1602 010000000011001011111110000000
1603 001000000011100101110111000000
1604 000100000011110010110011100000
1605 000010000011111001010001110000
1606 000001000011111100100000111000
1607 000000100001111110010000011100
1608 000000010010111111000000001110
1609 000000001001011111100000000111
1610 000000000100101111111000000011
1611 k= 10
1612 d= 8
1613
1614 Weight spectrum:
1615 8^10 9^20 10^20 11^40 12^60 13^140 14^165 15^112 16^165 17^140 18^60 19^40 20^20 21^20 22^10 30^1 |AUT|= 10 TRANS 0
1616 =====

```

```
1
2 ? 10 30 5 1 1
3 100000000030411330011130134104
4 010000000013041133004113013410
5 001000000001304113300411301341
6 000100000000130411331041130134
7 000010000030013041134104113013
8 000001000033001304113410411301
9 000000100013300130411341041130
10 000000010011330013040134104113
11 000000001041133001303013410411
12 000000000104113300131301341041
13 k: 10
14 information sets:
15 1: 3 4 5 6 7 8 9 10 29 30
16 2: 11 12 13 14 15 16 17 18 19 20
17 3: 1 2 21 22 23 24 25 26 27 28
18 Generetor matrices with different information sets:
19
20 ? 10 30 5 1 matrix N 1
21 111000000044201021310104443300
22 420100000041201342323132022300
23 340010000012200303113331442400
24 100001000013412134124040040400
25 020000100034332341414012012400
26 340000010043022320024311433000
27 140000001013003203310030031100
28 110000000142010213141044433000
29 010000000013041133004113013410
30 400000000020144220044420421401
31
32 ? 10 30 5 2 matrix N 2
33 444413423210000000002242342333
34 244441342301000000003224234233
35 3244441342001000000003322423423
36 2324444134000100000003332242342
37 423244441300001000002333224234
38 342324444100000100004233322423
39 134232444400000010003423332242
40 413423244400000001002342333224
41 441342324400000000104234233322
42 444134232400000000012423423332
43
44 ? 10 30 5 3 matrix N 3
45 104224013342240133100000000000
46 013310422433104224010000000000
47 003211111323113430241000000012
48 002342410130020244340100000032
49 000143011110141131400010000034
50 004001404132432410230001000010
51 001231132141003113420000100001
52 003243044114302303000000010043
53 002022013200411412130000001023
54 003231402342332240440000000121
55 d: 13
56
```





<b>Time:</b>	<b>Monday 7.12</b>	<b>Tuesday 8.12</b>
<b>15:00 - 15:20</b>	Opening	<b>N.Yankov</b> , Софтуер за Линкус и Уидоус от гледната точка на математика
<b>15:20 - 15:40</b>	<b>S.Bouyuklieva</b> , On-Line Encyclopedia of Integer Sequences and Coding Theory	<b>Dushan Bikov</b> , Parallel primitive Histogram and use in Cryptography
<b>15:40 - 16:00</b>	<b>Mariya Dzhumalieva-Stoeva</b> , Software for generating and classification of combinatorial designs and Hadamard matrices	<b>Valentin Bakoev</b> , The Combinatorial Algorithms in my Practice
<b>16:00 - 16:20</b>	<b>P.Boyvalenkov, M. Stoyanova</b> , Some LP bounds for covering radius of spherical designs	<b>I.Bouyukliev</b> , The program 'Equivalence' in the software package QextNewEdition
<b>Break</b>		
<b>16:40 - 17:00</b>	<b>S.Topalova, S.Zhelezova</b> , Finding putative automorphism groups of a parallelism of $PG(3,q)$ by GAP	<b>Z.Varbanov</b>
<b>17:00 - 17:20</b>	<b>S.Topalova, S.Zhelezova</b> , Invariants of resolutions of Steiner 2-designs.	<b>P. Piperkov</b> , Implementation through the Mathematica package of butterfly algorithms for determining the parameters of a linear code
<b>17:20 - 17:40</b>	<b>V. Monev</b>	<b>P. Kazakov</b>
<b>17:40 - 18:00</b>	Object oriented programming and mathematical software - disadvantages and advantages Compilers and Hardware – discussion	Good practices in the organization of experimental software for parallel and sequential implementation – discussion