

THE ON-LINE ENCYCLOPEDIA  
OF INTEGER SEQUENCES®

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founded in 1964 by N. J. A. Sloane

# On-Line Encyclopedia of Integer Sequences and Coding Theory

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# On-Line Encyclopedia of Integer Sequences (OEIS)

- The **On-Line Encyclopedia of Integer Sequences (OEIS)** also is an online database of **integer sequences**.
- It was created and maintained by **Neil Sloane**, while a researcher at **AT&T Labs**.
- He transferred the **intellectual property** and hosting of the OEIS to the **OEIS Foundation** in 2009. Sloane is president of the OEIS Foundation.

# Integer Sequences

- ✓ Sequence #1: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97, ... [A000040](#) The prime numbers.
- ✓ Sequence #2: 2, 3, 5, 7, 11, 101, 131, 151, 181, 191, 313, 353, 373, 383, 727, 757, 787, 797, 919, 929, ... [A002385](#) Palindromic primes: prime numbers whose decimal expansion is a palindrome.
- ✓ Sequence #3: 0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55, 89, 144, 233, 377, 610, 987, 1597, ... [A000045](#) Fibonacci numbers:  $F(n) = F(n-1) + F(n-2)$
- ✓ Sequence #4: 1, 2, 4, 7, 11, 16, 22, 29, 37, 46, 56, 67, 79, 92, 106, 121, 137, 154, ... [A000124](#) Central polygonal numbers  $n(n+1)/2 + 1$ ; or, maximal number of pieces formed when slicing a pancake with  $n$  cuts.
- ✓ Sequence #5: 1, -3, -8, -3, -24, 24, -48, -3, -8, 72, -120, 24, -168, 144, ... [A046970](#) Dirichlet inverse of the Jordan function  $J_2$

# Integer Sequences

✓ A000001. Number of groups of order  $n$ .

0, 1, 1, 1, 2, 1, 2, 1, 5, 2, 2, 1, 5, 1, 2, 1, 14, 1, 5, 1, 5, 2, 2, 1, 15, 2, 2, 5, 4, 1, 4, 1, 51, 1, 2, 1, 14, 1, 2, 2, 14, 1, 6, 1, 4, 2, 2, 1, 52, 2, 5, 1, 5, 1, ...

✓ A000010. Euler totient function  $\phi(n)$ : count numbers  $\leq n$  and prime to  $n$ .

1, 1, 2, 2, 4, 2, 6, 4, 6, 4, 10, 4, 12, 6, 8, 8, 16, 6, 18, 8, 12, 10, 22, 8, 20, 12, 18, 12, 28, 8, 30, 16, 20, 16, 24, 12, 36, 18, 24, 16, 40, 12, 42, 20, ...

✓ A100000. Middle column of marks found on the oldest object with logical carvings, the 22000-year-old Ishango bone from the Congo.

3, 6, 4, 8, 10, 5, 5, 7

# OEIS – българският принос

Valentin Bakoev:

✓ A319511 (author) <https://oeis.org/A319511>

Triangle read by rows:  $T(n,k)$  is the number of Boolean functions on  $n$  variables having an algebraic degree equal to  $k$  (for  $n \geq 0$  and  $0 \leq k \leq n$ ).

✓ A305860 (author) <https://oeis.org/A305860>

Triangle read by rows, representing a family of sequences  $M(n)$ , for  $n = 0, 1, 2, \dots$ . The  $n$ -th row of the triangle consists of  $n+1$  integers, denoted by  $\#m(n,0), \#m(n,1), \dots, \#m(n,n)$ , which are the terms of the sequence  $M(n)$ . They are the serial numbers of  $n+1$  binary vectors of size  $2^n$ , denoted by  $m(n,0), m(n,1), \dots, m(n,n)$ , correspondingly. Each vector  $m(n,k)$  is a characteristic vector of all vectors from the  $n$ -dimensional Boolean cube (hypercube)  $\{0,1\}^n$ , having (Hamming) weight equal to  $k$ , for  $k = 0, 1, \dots, n$ , and for  $n > 0$ . The zero row (i.e.,  $M(0)$ ) and its single term 1 are prepended for convenience.

✓ A294648 (author) <https://oeis.org/A294648>

Irregular triangle read by rows, representing a family of sequences  $L(n)$ , for  $n=1, 2, 3, \dots$ . The sequence  $L(n)$  (i.e. the  $n$ -th row) is the ordinance of vectors of the  $n$ -dimensional Boolean cube (hypercube)  $\{0,1\}^n$  in accordance with their (Hamming) weights, where the lexicographic order is chosen as a second criterion for an ordinance the vectors of equal weights.

# OEIS – българският принос

- Krassimir Atanassov - [Institute of Biophysics and Biomedical Engineering, Bulgarian Academy of Sciences](#)
- Head of Department “Bioinformatics and Mathematical Modelling” (since Jul 2010)
- **Notes on Number Theory and Discrete Mathematics**

<http://nntdm.net/>

# OEIS and Coding Theory

- <https://oeis.org/A034356>

Triangle read by rows giving  $T(n,k)$  = number of inequivalent linear  $[n,k]$  binary codes ( $n \geq 1, 1 \leq k \leq n$ ).

- <https://oeis.org/A003179>

Number of self-dual binary codes of length  $2n$  (up to column permutation equivalence).

# Таблицы и редици от наши публикации

Таблица 1.1: Двоични самодуални кодове с дължина  $n \leq 36$  [83]

$n$	$\#I$	$\#II$	$d_{max,I}$	$\#_{max,I}$	$d_{max,II}$	$\#_{max,II}$	Литература
2	1		$2^O$	1			[115]
4	1		$2^O$	1			[115]
6	1		$2^O$	1			[115]
8	1	1	$2^O$	1	$4^E$	1	[115]
10	2		$2^O$	2			[115]
12	3		$4^E$	1			[115]
14	4		$4^E$	1			[115]
16	5	2	$4^E$	1	$4^E$	2	[115]
18	9		$4^E$	2			[115]
20	16		$4^E$	7			[115]
22	25		$6^E$	1			[119]
24	46	9	$6^E$	1	$8^E$	1	[119]
26	103		$6^O$	1			[37, 40, 116]
28	261		$6^O$	3			[37, 40, 116]
30	731		$6^O$	13			[37, 40, 116]
32	3210	85	$8^E$	3	$8^E$	5	[16, 37, 41]
34	24147		$6^O$	938			[15]
36	?		$8^E$	41			[59]



# Таблицы и редици от наши публикации

## The number of binary SD codes

$n$	$\#I$	$\#II$	$d_{max,I}$	$\#_{max,I}$	$d_{max,II}$	$\#_{max,II}$
24	46	9	6	1	8	1
26	103		6	1		
28	261		6	3		
30	731		6	13		
32	3 210	85	8	3	8	5
34	24 147		6	938		
36	519 492		8	41		
38	38 682 183*BB		8	2 744		
40	<b>8 250 058 081</b>	94 343	8	10 200 655*BBH	8	16 470

\*BBH - Bouyuklieva, Bouyukliev, Harada

\*BDM - Bouyukliev, Dzhumalieva-Stoeva, Monev

# Таблицы и редици от наши публикации

Table 1: Classification of binary self-orthogonal codes

$n \backslash k$	3	4	5	6	7	8	9	10
7	4 1							
8	4 1	4 1						
9	4 1	4 0						
10	4 3	4 3						
11	4 2	4 2	4 1					
12	6 1	4 10	4 5	4 1				
13	6 1	4 6	4 5	4 1				
14	8 1	6 2	4 22	4 10	4 1			
15	8 1	8 1	6 1	4 13	4 3			
16	8 3	8 2	8 1	6 1	4 20	4 3		
17	8 3	8 2	8 1	6 2	4 37	4 4		
18	8 8	8 10	8 5	8 2	6 3	4 45	4 2	
19	10 1	8 12	8 10	8 2	8 1	6 1	4 12	
20	10 2	8 50	8 50	8 23	8 4	8 1	6 1	4 7
21	12 1	10 1	8 101	8 57	8 15	8 2	8 1	6 1
22	12 1	10 6	8 417	8 416	8 117	8 16	8 2	8 1
23	12 3	12 1	10 2	8 1729	8 848	8 104	8 12	8 2
24	12 6	12 4	12 1	10 1	8 9839	8 1824	8 124	8 16
25	12 8	12 6	12 2	10 27	8 96560	8 37625	8 1891	8 60
26	14 1	12 27	12 13	12 2	10 26	8	8	8 1689
27	14 2	12 48	12 60	12 24	12 1	10 1	8	8
28	16 1	14 1	12 345	12 383	12 61	10 43579	8	8
29	16 1	14 3	12 1507	12 4468	12 5694	12 73	10	8
30	16 3	16 1	14 3	12	12	12	12 9	10
31	16 6	16 2	16 1	12	12	12	12	12 2
32	16 12	16 9	16 3	16 1	12	12	12	12
33	18 1	16 16	16 8	16 0	12	12	12	12
34	18 2	16 71	16 63	16 15	14 5399	12	12	12
35	20 1	16 152	16 380	16 362	16 4	14	12	12
36	20 1	18 2	16 2876	16 20392	16 7484	16 2	14	12
37	20 3	18 8	16 17705	16	16	16	14	14
38	20 6	20 1	18 3	16	16	16	16 47	14
39	20 12	20 4	18 50	16	16	16	16	14
40	22 1	20 17	20 3	18 41	16	16	16	16

# Таблицы и редици от наши публикации

$n/k$	2	3	4	5	6	7	8	9	10	11	12	13
5	1											
6	3	1										
7	4	4	1									
8	6	10	5									
9	8	23	23	5								
10	10	42	76	41	4							
11	12	71	207	227	60	3						
12	15	115	509	1012	636	86	2					
13	17	174	1127	3813	4932	1705	110	1				
14	20	255	2340	12836	31559	24998	4467	127	1			
15	23	364	4606	39750	176582	293871	132914	11507	143	1		
16	26	505	8685	115281	896316	2955644	3048590	733778	28947	144		
17	29	686	15797	317464	4226887	26590999	58085499	34053980	4115973	70455	129	
18	33	919	27907	837697	18807438	220135857	971007974	1261661451	393087258	27333440	293458	113

TABLE I  
THE NUMBER OF INEQUIVALENT  $[n, k, d \geq 3]_2$  CODES FOR  $n \leq 18$

$k$	4	5	6	7	8	9	10	11	12	13
#	8561	129586	1813958	16021319	60803805	73340021	22198835	1314705	11341	24

TABLE II  
THE NUMBER OF INEQUIVALENT EVEN  $[n, k, d \geq 4]_2$  CODES FOR  $n \leq 19$  AND  $k \geq 4$

$k$	3	4	5	6	7	8	10	11
#	726	12817	358997	11697757	246537467	1697180017	62180809	738

TABLE III  
THE NUMBER OF EVEN  $[n \leq 21, k, d \geq 6]_2$  CODES FOR  $3 \leq k \leq 11, k \neq 9$